



The adsorption of chlorofluoromethane on pristine, and Al- and Ga-doped boron nitride nanosheets: a DFT, NBO, and QTAIM study

Mohsen Doust Mohammadi¹ · Hewa Y. Abdullah²

Received: 17 July 2020 / Accepted: 17 September 2020
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Abstract

In the present investigation, the feasibility of detecting the chlorofluoromethane (CFM) gas molecule onto the outer surface of pristine single layer boron nitride nanosheet (BNNS), as well as its aluminum (Al)- and gallium (Ga)-doped structures, was carefully evaluated. For achieving this goal, a density functional theory level of study using the Perdew, Burke, and Ernzerhof exchange–correlation (PBE/PBE) functional together with a 6-311G(d) basis set has been used. Subsequently, the B3LYP, CAM-B3LYP, wB97XD, and M062X functionals with a 6-311G(d) basis set were also employed to consider the single-point energies. Natural bond orbital (NBO) and quantum theory of atoms in molecules (QTAIM) were implemented by using the B3LYP-D3/6-311G(d) method, and the results were compatible with the electronic properties. In this regard, the total density of states (TDOSs), the Wiberg bond index (WBI), natural charge, natural electron configuration, donor–acceptor natural bond orbital interactions, and the second-order perturbation energies are performed to explore the nature of the intermolecular interactions. All of the energy calculations and population analyses denote that by adsorbing of the gas molecule onto the surface of the considered nanostructures, the intermolecular interactions are of the type of strong chemical adsorption. Among the doped nanosheets, Ga-doped nanosheet has very high adsorption energy compared with other elements (i.e., Ga-doped > Al-doped > pristine). Generally, it was revealed that the sensitivity of the adsorption will be increased when the gas molecule interacts with decorated nanosheets and decrease the HOMO-LUMO band gap; therefore, the change of electronic properties can be used to design suitable nanosensors to detect CFM gas.

Keywords Chlorofluoromethane · CFM · Boron nitride · Nanosheet · Density functional theory · Freon 31 · Natural bond orbital

Introduction

In the last two decades, theoretical studies in the density functional theory (DFT) framework on nanostructures have attracted the attention of many scientists in the fields of computational chemistry and solid-state physics [1–9]. The study of boron nitride nanosheet is no exception, and many theoretical studies on this nanostructure have led to interesting proposals for the manufacture of industrial devices [10–13]. Azizi et al. showed that when H₂O molecule placed on the VD-

8*8BNNS cavity, it will dissociatively chemisorbed [14]. Esrafil et al. have investigated widely various theoretical researches in order to adsorb different molecules such as NO [15], CO [16], CH₂O [4], COCl₂ [17], C₂H₄ [18], and N₂O [19] on the surface of pristine and decorated boron nitride nanosheet. Mohammadi et al. have studied the adsorption of halomethanes onto the BN, Al/Ga-doped nanosheets [7]. Rossini et al. showed the characterization of *h*-BNNS molecular edge terminations [20]. Shao et al. used BNNS@Ti₃C₂ as an electrocatalyst [21]. Joo et al. had an interesting simulation for the separation of copper and mercury using BNNS [22], and many other researches, all of which cannot be mentioned here [23–26]. The widespread use of boron nitride nanosheets provides the basis for further study on such structures.

Chlorofluoromethane (CFM) (also known as Freon 31 or HCFC 31 with chemical formula CH₂ClF) is classified as a category 2 carcinogen from the group of chlorofluorocarbons or dihalomethanes. It is a colorless, odorless, flammable gas

✉ Hewa Y. Abdullah
hewayaseen@gmail.com

¹ School of Chemistry, College of Science, University of Tehran, Tehran 14176, Iran

² Physics Education Department, Faculty of Education, Tishk International University, Erbil 44001, Iraq

with a solid monoclinic crystal structure of space group P21 [27]. Chlorofluoromethane was used as the refrigerant. It is listed in the Montreal Protocol as a substance that degrades the ozone layer [28]. A rotational study has been performed by Caminati et al. [29] to investigate the dimer interactions of CFM molecule, and the results confirm that the interactions are non-covalent. According to the dissociation energy of dimer complex of CMF molecule reported in [29], we considered it as an isolated single molecule in this work.

This article discusses the design of such a sensor. This study investigated the interactions of CFM with BNNS and BN nanosheets doped with Al and Ga elements. After optimizing the structure of boron nitride nanosheets by Gaussian software, to study the chemical stability and conductivity, the element doping process on this nanosheet has been studied. Because of the high sensitivity of computation to precisely determine the energy of molecular orbitals to investigate the conductivity and probability of physical and chemical adsorption, different structures need to be optimized using appropriate computational methods. For this purpose, the PBEPBE functional and 6-311G(d) basis set was used in this research for computation. The B3LYP, CAM-B3LYP, wB97XD, and M062X functionals with 6-311G(d) basis set were also used to calculate the single-point energies. Natural bond orbital and quantum theory of atoms in molecules were studied by using the PBEPBE/6-311G(d) method, and the results were used to obtain various physical parameters. Our results show that we can devise a gas sensor to detect CMF by using the pristine, and Al- and Ga-doped BNNS.

Computational details

The DFT calculations at Perdew, Burke, and Ernzerhof (PBE-PBE) functional [30] together with 6-311G(d) Pople split-valence triple-zeta basis set with polarization functions [31] were used for geometry optimization for all different positions of the CFM/sheet complex structures. To determine the stability of the optimized structures, frequency calculations are also performed using the similar level of theory to approve that all the stationary points are in agreement with a minimum point through the potential energy surface. For further investigation, single-point energy calculations using different levels of theory were also applied on the most stable relaxed structures, which were obtained from geometry optimization at the PBEPBE/6-311G(d) level. The levels of theory used for the single-point energy calculations included B3LYP-D3, M06-2X, and wB97XD together with 6-311G(d) basis set. Natural bond orbital (NBO) and quantum theory of atoms in molecules (QTAIM) were implemented by using the B3LYP-D3/6-311G(d) method. All of the calculations including geometry optimization, single-point energy calculations, and NBO analysis were performed by Gaussian 16 package [32]. It should

be noted that the NBO calculations were performed using NBO v 3.0 software which is embedded within Gaussian software. In order to perform quantum theory of atoms in molecule (QTAIM) and density of state (DOS) analyses, the Multiwfn program [33–35] was employed.

The adsorption energy (E_{ads}) of the investigated CFM onto the surface of the pristine and doped nanosheets can be calculated as follows:

$$E_{\text{ads}} = E_{\text{sheet/CFM}} - (E_{\text{sheet}} + E_{\text{CFM}}) \quad (1)$$

where $E_{\text{sheet/CFM}}$ represents the total energy of the complex structure. E_{sheet} and E_{CFM} are the total energies of the pure nanosheet and the pure CFM molecule, respectively. Note that the absorption energy consists of two parts, namely the interaction energy (E_{int}) and the deformation energy (E_{def}) that occur in the absorption process. Therefore, the following equations are used to calculate these proportions:

$$E_{\text{ads}} = E_{\text{int}} + E_{\text{def}} \quad (2)$$

$$E_{\text{int}} = E_{\text{sheet/CFM}} - E_{\text{sheetincomplex}} - E_{\text{CFMincomplex}} \quad (3)$$

$$E_{\text{def}} = E_{\text{def}}^{\text{sheet}} + E_{\text{def}}^{\text{CFM}} = (E_{\text{sheetincomplex}} - E_{\text{pristin-sheet}}) + (E_{\text{CFMincomplex}} - E_{\text{isolatedCFM}}) \quad (4)$$

where $E_{\text{sheet in complex}}$ and $E_{\text{CFM in complex}}$ are energies of CFM molecule and nanosheet in the optimized complexes, respectively.

Results and discussion

The structural analysis

To optimize the structure of pristine single layer boron nitride nanosheets using periodic boundary conditions, we select a 2D unit cell of boron and nitrogen atoms which is $a = 10.0042 \text{ \AA}$ and $b = 10.0043 \text{ \AA}$ in length containing 32 atoms. We optimized this nanosheet by DFT method with PBEPBE functional together with basis set 6-311G (d). After optimization of the pristine nanosheet, we substituted Al and Ga with B atom; then, the optimization process has been repeated for doped nanosheets. The quantitative values of bond lengths are shown in Fig. 1.

The next step was the optimization of CFM/nanosheet complexes. In this step the CFM molecule was placed on the outer surface of each abovementioned nanosheets with vertical distance of about 2.1 \AA . To find out the optimum distances between nanosheet and CFM molecule, we used the rigid scan for some cases to estimate the most efficient distance. It should be noted that the level of theory in both optimization and rigid scan was PBEPBE/6-311G (d). To better explain the

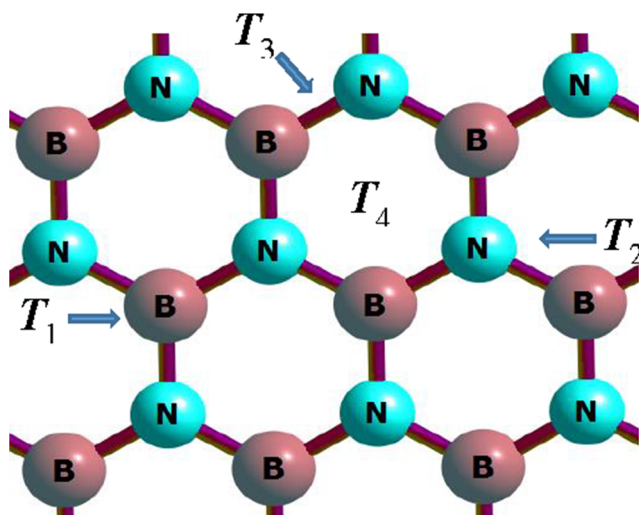


Fig. 3 All possible target positions for the adsorption of any arbitrary molecules onto the surface of BNNS. Top of boron atom (T_1), top of nitrogen atom (T_2), between boron and nitrogen atoms (T_3), and top of the hexagonal ring (T_4)

negligible difference among the adsorption energies; therefore, the boron atom position was the target position on the BN nanosheet.

In the next step, the nanosheet is expanded three times in each direction ($a = 25.85 \text{ \AA}$, $b = 25.92 \text{ \AA}$) and terminated with hydrogen atom. Since the PBE/PBE functional does not account for the scattering contribution, it is expected that in poor interactions, this functional will not give a good estimate of the amount of energy. For this reason, methods have been developed for effects. One of the most effective, accurate, and low computational methods is the experimental method developed by Grimme et al. This method is highly accurate because it has an empirical basis and its parameters are extracted from the spectroscopic experimental data. Various versions of the semi-empirical Grimme method have been presented in recent years [37–39]. In this work we used the latest version of B3LYP-D3 known as D3 (BD) (GD3BJ), and wB97XD to consider long range and dispersion effects.

Single-point energy calculations using different functional such as B3LYP-D3, wB97XD, and M062X and 6-311G(d) basis set were done. The calculated values indicate a strong interaction between nanosheets and CFM molecule. Since the PBE-PBE functional does not account for the long-range scattering contribution, it is expected that in poor interactions, this functional will not give a good estimate of the amount of energy. For this reason, methods have been developed for long range and dispersion effects. In this work we used B3LYP-D3 and wB97XD to consider long range and dispersion effects. The well-known M062X functional is used for better comparison. The results show that the energies obtained from the PBE/PBE and other functionals are consistent with the accuracy of the calculations. On the other hand, as expected, the B3LYP-D3 method shows more energy values than

the others, due to the dispersion contribution consideration. Also by doping the Al and Ga elements on the BN nanosheet, significant changes in the results are achieved. Table 1 shows that doping Al and Ga increases the absorption energy and enhanced the chemical absorption. Table 2 also shows the bond length and the nearest intermolecular distances (re (\AA)) between CFM molecule and BNNS, BNAlNS, and BNGaNS (Fig. 4).

Energetics properties

The chemical electron potential (μ) describes the tendency of electrons to escape from a particular species at the ground state. This quantity is equal to the absolute negative electro-negativity obtained from the definition provided by Mulliken, as follows:

$$\mu = -\chi \quad (5)$$

Parr and his colleagues [40] used the DFT to show that at a constant external potential, the potential energy of an electron is related to the first derivative of energy relative to the number of electrons, as follows:

$$\mu = \left(\frac{\partial E}{\partial N} \right)_{v(r)} = -\frac{1}{2}(IP + EA) \quad (6)$$

where IP and EA are the ionization affinity and electron affinity, respectively [41]. Based on the Koopmans' approximation (see the Hartree–Fock theory) and Janak's approximation [42] (in the DFT theory), the ionization and electron affinity potentials are equal to the negative value of the highest occupied molecular orbital (HOMO) energy ($\varepsilon_{HOMO} = -IP$) and negative value of the lowest unoccupied molecular orbital (LUMO) ($\varepsilon_{LUMO} = -EA$). Therefore, the chemical potential in Janak's approximation is defined as

$$\mu = \left(\frac{\partial E}{\partial N} \right)_{v(r)} \cong \frac{(\varepsilon_{LUMO} + \varepsilon_{HOMO})}{2} \quad (7)$$

where ε_{HOMO} and ε_{LUMO} are the energies of the HOMO and the LUMO, respectively. N is the number of electrons, E is the total electronic energy of the system, and $v(r)$ is the external potential.

Comparison of the variation in electron chemical potentials to that in the number of electrons at a constant external potential is called chemical hardness, which is expressed as

$$\eta = \left(\frac{\partial \mu}{\partial N} \right) = \frac{1}{2} \left(\frac{\partial^2 E}{\partial N^2} \right) \quad (8)$$

Parr et al. [43] used the electron energy curve as well as the finite difference approximation to express hardness as follows:

Table 1 The adsorption energies (E_{ads}) and deformation energies (E_{def}) for BNNS, BNAINS, and BNGaNS with CFM molecule. All values are in (eV)

Systems	PBEPBE		B3LYP-D3		M06-2X		wB97XD	
	E_{ads}	E_{def}	E_{ads}	E_{def}	E_{ads}	E_{def}	E_{ads}	E_{def}
CH ₂ ClF/BNNT	− 0.163	0.003	− 0.386	0.011	− 0.247	0.009	− 0.364	0.015
CH ₂ ClF/BN(Al)NT	− 1.043	0.021	− 1.330	0.031	− 1.195	0.018	− 1.270	0.028
CH ₂ ClF/BN(Ga)NT	− 1.085	0.027	− 1.342	0.025	− 1.343	0.029	− 1.280	0.035

$$\eta = \frac{1}{2} (IP - EA) \quad (9)$$

Moreover, using Janak and Koopman's approximations, the hardness equation is transformed as follows:

$$\Delta E_{\text{min}} = -\frac{\mu^2}{2\eta} \quad (10)$$

Chemical hardness is the energy gap between the HOMO and the LUMO. Therefore, molecules with high energies are considered hard molecules, while those with low energies are called soft molecules. Since the softness of a molecule is the opposite of its hardness, the equation for molecule softness is denoted as follows [44]:

$$S = \frac{1}{\eta} \quad (11)$$

Inspired by Maynard's work, Parr et al. [45] introduced electrophilicity as the steady-state energy in which an atom or a molecule at ground state gains by receiving additional electron charges from the environment. The energy changes that lead to such a charge transfer are expressed as follows:

$$\Delta E = \mu \Delta N + \frac{1}{2} \eta (\Delta N)^2 \quad (12)$$

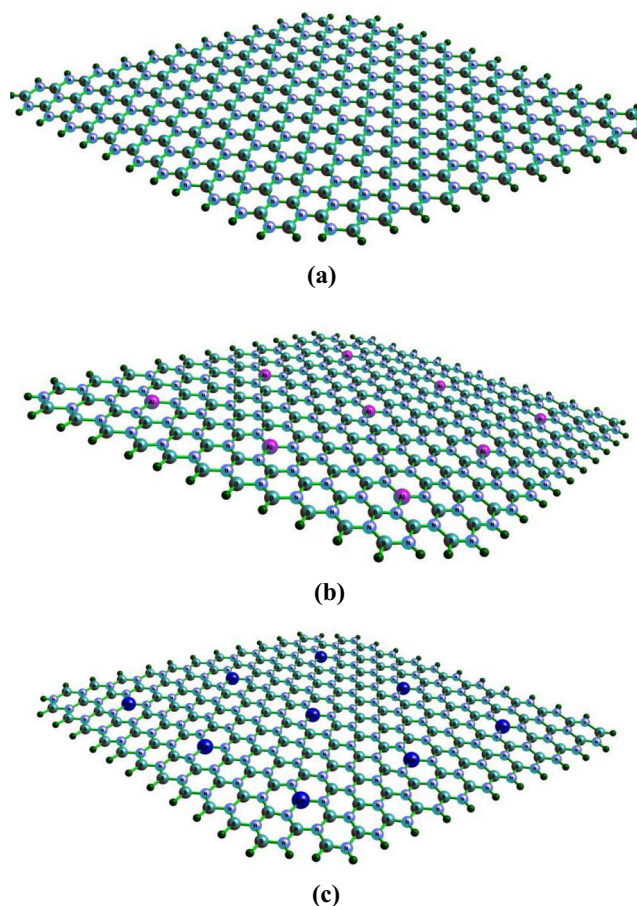
When the system receives electron charges from the environment sufficient to equate its potential to that of the environment, the system is saturated with electrons and can be expressed as follows:

$$\frac{d\Delta E}{d\Delta N} = 0 \quad (13)$$

The electron load received from the environment is maximized, and the total energy of the system is eventually minimized. Thus,

$$\Delta N_{\text{max}} = -\frac{\mu}{\eta} \quad (14)$$

$$\Delta E_{\text{min}} = -\frac{\mu^2}{2\eta} \quad (15)$$

**Fig. 4** The 2D **a** boron nitride, **b** Al-doped boron nitride, and **c** Ga-doped boron nitride nanosheets terminated with hydrogen atoms**Table 2** The bond lengths and the nearest intermolecular distances (re (Å)) between CFM molecule and BNNS, BNAINS, and BNGaNS. All calculations were performed using PBC-DFT PBEPBE/6-311G(d) level of theory (x = Al and Ga)

Systems	F.... (x)	F....B	F....N	C-F	C-Cl	C-H
CH ₂ ClF/BNNS	-	3.014	3.297	1.371	1.802	1.101
CH ₂ ClF/BNAINS	2.036	3.855	4.084	1.458	1.751	1.096
CH ₂ ClF/BNGaNS	2.124	3.876	3.225	1.435	1.762	1.097

Since $\eta > 0$, $\Delta E < 0$ always, and the charge transfer is energetically desirable. Accordingly, Parr et al. proposed the following equation to denote the electrophilicity of electrophilic species.

$$\omega = \frac{\mu^2}{2\eta} \quad (16)$$

In fact, the electrophilicity index is the capacity of a species to accept an arbitrary number of electrons from the environment. In this regard, Nourizadeh and Maihami [46] used electrophilicity in the Diels–Alder reaction and stated that “atoms appear to be arranged in a natural tendency to reach the lowest electrophilicity.” This expression is called the minimum electrophilicity principle (MEP).

The values of maximum occupied molecular orbital (HOMO) and lowest occupied atomic orbital (LUMO) and their differences (HLG), chemical potential (μ), chemical hardness (η), and electrophilicity (ω) are reported in Table 3. From the results of this table, it can be seen that by adsorption of CFM molecule onto the outer surface of nanosheets, the distance between HOMO and LUMO levels is reduced relative to the pure nanosheet, which shows the greatest decrease in the interaction of the Al-doped boron nitrogen nanosheet and CFM, which is caused by the molecular energy absorption matched from this position. By doping the elements Al and Ga, it is observed that HLG changed. The decrease in HLG results in an increase in the electrical conductivity and thus an increase in the metal property of all the nanosheets compared with pure BNNS. It is also noteworthy that the observed changes in HLG after doped Al and Ga are mainly due to lower LUMO energy levels. In order to study these changes in the electron structure of the studied cases more closely, the density of state spectra (DOS) will be analyzed in the next section. For a more detailed study of the electron structure changes, the density of state spectra (DOS) is extracted and illustrated in Fig. 5.

From the DOS spectra, it is clear that DOS spectra for all absorption are in agreement with the values of the energy

parameters reported in Table 3. The lowest amount of adsorption energy is related to the pristine nanosheet, and the highest amount of adsorption energy is for the adsorption of CFM onto the Al-doped BN nanosheet; the most changes are also observed in the DOS spectrum relative to the Al-doped nanosheet. In other words, the electron structure changes show a direct relationship with the absorption energies. Given the amount of absorption energy, high amount of binding energy, and the structure of DOS spectra obtained in all of these cases, it can be claimed that the adsorption of CFM molecule onto BN, BN (Al), and BN (Ga) nanosheets is a strong physical adsorption type.

NBO and QTAIM analyses

The natural bond orbital (NBO) analysis has been developed based on many-electron molecular wavefunction in terms of localized electron-pair bonding units and uses first-order reduced density matrix of the wavefunction [47, 48]. In the NBO approach, a given wavefunction should be transformed into a localized form in which NBOs are considered local block eigenfunctions of the density matrix. NBO analysis is applicable in both closed-shell and open-shell systems which are calculated from atom-centered basis functions [49]. The mechanism of the energetic analysis of NBO interactions is based on the one-electron effective energy operator (Fock or Kohn–Sham matrix) that arises from the host electronic structure system (ESS). Second-order perturbation theory is one of the highest uses methods for estimating energy effects. For the case of HF or DFT methods, the interactions between NBOs are considered to analyze the wavefunction energetically, with the explanation that the Kohn–Sham matrix elements [50–60].

We used the B3LYP/DEF2-QZVP level of theory to perform the NBO calculations. The concept of bonded orbitals can be used to understand the distribution of electrons in atomic and molecular orbitals. Atomic charges and molecular bonds can be used to obtain these orbitals. In this method, an electron density matrix is used to both define the shapes of the atomic orbitals in the molecular environment and obtain molecular bonds (electron density between atoms). NBO is defined as the following equation for σ bonding between atoms A and B.

$$\sigma_{AB} = C_A h_A + C_B h_B \quad (17)$$

where h_A and h_B are natural hybrids on the A and B atoms. In the covalent limit, $C_A = C_B$, and at the ionic limit, $C_A \gg C_B$ (if the electronegativity of A is greater than B). Each bonding NBO must be paired with a corresponding anti-bonding NBO.

$$\sigma^*_{AB} = C_A h_A - C_B h_B \quad (18)$$

Binding orbital analysis is used to evaluate the effects of non-stationary effects, such as anomeric effect,

Table 3 Values of HOMO energy (ϵ_H), LUMO energy (ϵ_L), HOMO and LUMO energy gap (HLG), chemical potential (μ), chemical hardness (η), and electrophilicity (ω). All values are in (eV) and were obtained from completed nanosheet B3LYP-D3/6-311G(d) level of theory

Systems	ϵ_H	ϵ_L	HLG	μ	η	ω
BNNS	-6.374	-0.446	5.929	-3.310	2.864	15.692
BNAINS	-6.177	-0.437	5.739	-3.307	2.870	15.692
BNGaNS	-6.180	-0.438	5.742	-3.309	2.871	15.716
CBrClF2/BNNS	-6.355	-0.448	5.907	-3.301	2.854	15.550
CBrClF2/BNAINS	-6.084	-0.541	5.543	-3.313	2.772	15.208
CBrClF2/BNGaNS	-6.105	-0.425	5.680	-3.265	2.840	15.137

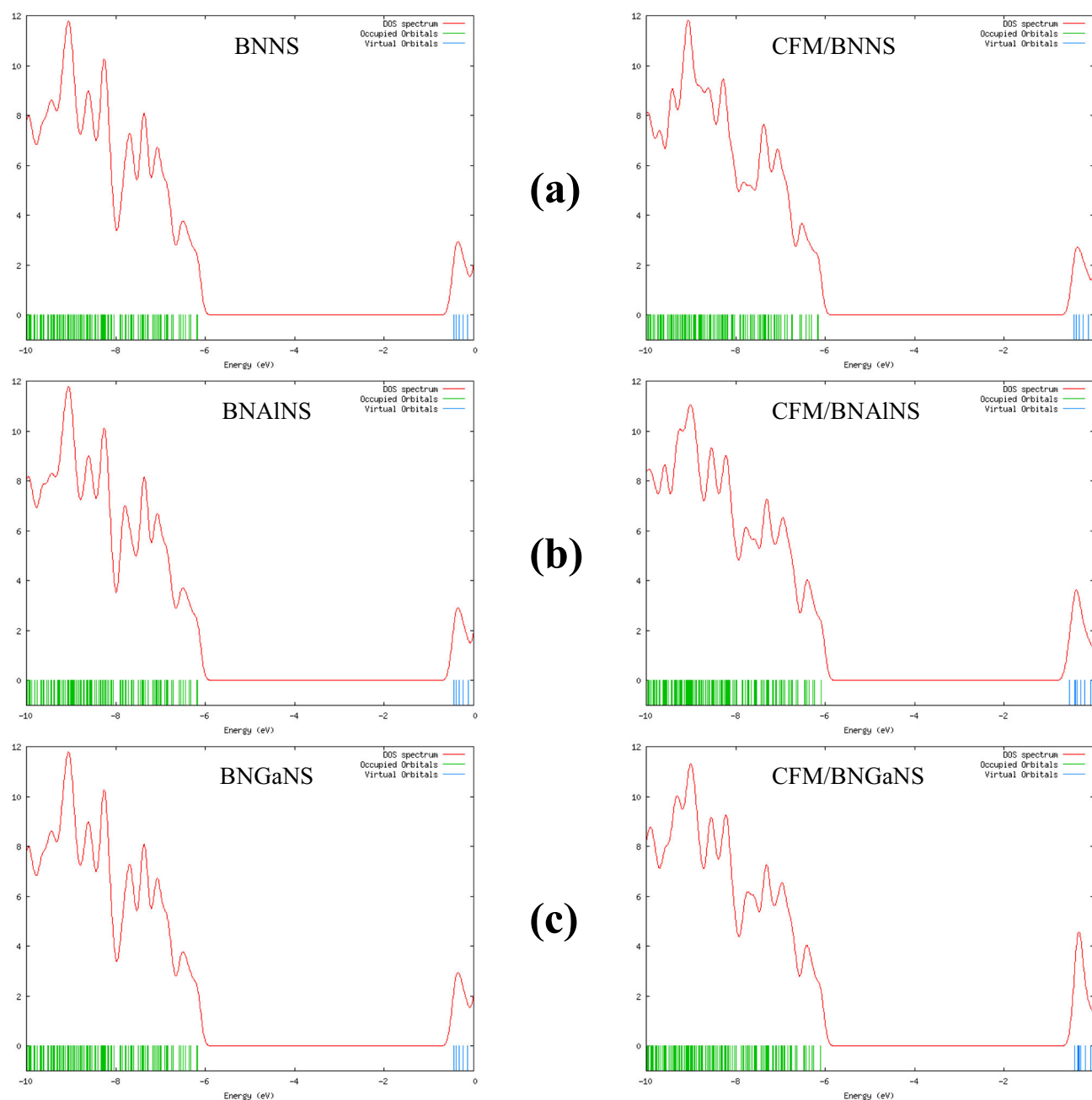


Fig. 5 The density of state (DOS) diagrams for the adsorption of CFM molecule onto the surface of the **a** pristine, **b** Al-doped, **c** Ga-doped boron nitride nanosheets. The data were obtained from completed nanosheet

and B3LYP-D3/6-311G(d) level of theory. The left side diagrams are isolated nanosheets, and the right side diagrams are CFM/nanosheet clusters

rotation barrier, and hydrogen bonding. In NBO analysis, molecular energy is divided into two parts: total energy (for non-stationary enters) and Lewis molecule energy (where super-conjugation does not occur, and the electrons are strongly bound in single bonds and pairs). The occupied NBOs describe the covalent effects in the molecule, while the non-occupied NBOs are used to describe non-covalent effects. The most important non-occupied NBOs are anti-bond orbitals [47, 59, 60].

Various types of bond order analyses are developed to take into account the bond property such as Mulliken bond order analysis [61], Mayer bond order analysis [62, 63], multi-center bond order analysis [64, 65], Wiberg bond order analysis [66], and fuzzy bond order [67, 68]. Due to the different assumptions, caution should be exercised when using the abovementioned methods and the term “Caveat emptor” in this case is a practical example to describe such a situation. Basis set containing diffuse functions as case in point leads to unreliable result for Mulliken or Mayer analyses [33].

According to the literature [69], the Wiberg bond order, in comparison to the Mayer method, has much less sensitivity to the basis set. The Wiberg bond index (WBI) is the sum of squares of off-diagonal density matrix elements between atoms and is denoted as follows:

$$\text{WBI} = \sum_k p_{jk}^2 = 2p_{jj}p_{jk}^2 \quad (19)$$

where P_{jk} represents the density matrix elements (i.e., the contribution of interactions between basis functions j and k) and P_{jj} is the charge density in the atomic orbital. In the WBI, there is no difference between net bonding or antibonding type of elements of the density matrix.

NBO analysis was used to calculate the bond order using the Wiberg method [66] for a more detailed examination of the types of interactions. After studying the adsorption energy of the complexes, we examine the bond length and bond order of the gases and the nanosheets before and after the adsorption. The Wiberg bond order for these clusters is reported in Table 4. According to this table, that the bond of the halogen atoms in CFM molecules oriented to the N in BNNS, Al in BNAINS and Ga in GaNNS are the most significant bonds. The results of the WBI analysis agree with the adsorption energies reported in Table 1. They reveal that these nanosheets show a strong interaction with the gas molecules and can be considered a suitable sensor for such gases.

One of the results of the natural population analysis obtained from NBO calculation is a natural electron configuration which shows the effective valence electron configuration for any atoms in the studied structure. The results of the NBO calculations shed light on the natural electron configuration and partial natural charge, which are useful in the study of the character of the bond between the CFM and the nanosheets. The NBO approach was implemented for all atoms in the pristine and cluster systems to reveal the quantities listed in Table 5. Charge transfer quantity between CFM molecule and nanosheets can also be a criteria to study the interaction of nanosheet and CFM, such that the stronger the interaction, the more the charge transfer between CFM and the nanosheet. Table 5 shows that there is a significant charge transfer between two species during adsorption process.

Table 4 The Wiberg bond index (WBI), obtained for atomic bonds and intermolecular interactions between CFM molecule and BNNS, BNAINS, and BNGaNS. All calculations were performed using B3LYP-D3/6-311G(d) level of theory

Systems	F.... (x)	F....B	F....N	C-F	Cl....F	H....F
CH ₂ ClF/BNNS	-	0.001	0.002	0.872	0.072	0.022
CH ₂ ClF/BNAINS	0.200	0.001	0.008	0.725	0.061	0.012
CH ₂ ClF/BNGaNS	0.188	0.001	0.010	0.756	0.063	0.014

In addition, by implementing the natural electron configuration, the type of the interaction between nanosheets and CFM molecule will be described. From Table 5 it can be obvious that valance configuration of isolated CFM molecule and nanosheets as well as valance configuration of nanosheet/CFM clusters have been increased. Therefore, the interaction of CFM with all nanosheets can be classified as a strong chemisorption process.

The second-order perturbation is an estimation of donor-acceptor interactions in the NBO basis. NBO analysis expresses the complex quantum-mechanical wavefunction into a more palpable Lewis-dot-like formalism. Lewis-type NBOs are called filled or “donor” orbitals (σ), and non-Lewis-type NBOs are called vacant or “acceptor” orbitals (σ^*). For each donor NBO (i) and acceptor NBO (j), the stabilization energy $E(2)$ is calculated as follow [57]:

$$E(2) = \Delta E_{ij}^2 = -q_i \frac{(F_{i,j})^2}{(\varepsilon_j - \varepsilon_i)} \quad (20)$$

where ε_i and ε_j are diagonal elements which show the orbital energies, q_i denotes the donor orbital occupancy ($q = 2$ for closed-shell systems and $q = 1$ for open-shell systems), and the off-diagonal NBO Fock matrix element is demonstrated by $F(i,j)$, and ΔE_{ij}^2 is the stabilization energy.

The results of electron donor-acceptor electron configuration of pristine BNNS and doped BN (Al), and BN (Ga) nanosheets are reported in Table 6. It is noteworthy that in this table the most important interactions in terms of the electron transfer stability energy are reported. The existence of such interactions with the remarkable stability energies in this table shows that in all cases the doped atom has been incorporated into the nanosheet structure by the chemical interaction and the stability structure has been achieved. In other words, the inserted atom behaves as a doping atom. The data in Table 6 show that the most important interaction for the pristine nanosheet related to electron transfer from the BD (B–N) bond as the electron donor to the BD*(C–F) as the receptor. This is in agreement with the results of the absorption energy as well as with the other results which have been examined. In the study of the doped complexes, it is observed that in the Al-complex, the Al electron pair is the Al receptor (Lewis acid) and the N-bonded electron pair is the amino group of the electron donor molecule (Lewis base). The highest electron-acceptor stabilization energy in all cases is due to the same interaction, which indicates a strong adsorption of the molecule onto the BN (Al) nanosheet compared with the others.

QTAIM analysis

QTAIM is a powerful tool for topology analysis containing the type and structure of bonds and intermolecular

Table 5 Natural electron configurations and natural charges (au) for the isolated CFM, pristine and Al- and Ga-doped nanosheets and their complex structures. All values calculated by the PBEPBE/6-311G(d) level of theory

Systems	Atom	Natural charge	Natural electron configuration
BNNS	B	1.18	[core]2S(0.63)2p(1.52)3p(0.01)3d(0.01)
	N	− 1.18	[core]2S(1.35)2p(4.82)
BNAINS	B	1.18	[core]2S(0.63)2p(1.52)3p(0.01)3d(0.01)
	N	− 1.18	[core]2S(1.37)2p(4.75)
BNGaNS	Al	2.01	[core]3S(0.40)3p(0.58)3d(0.02)
	B	1.18	[core]2S(0.63)2p(1.52)3p(0.01)3d(0.01)
	N	− 1.18	[core]2S(1.37)2p(4.75)
CH ₂ ClF/BNNS	Ga	1.80	[core]4S(0.56)4p(0.66)4d(0.01)
	B	1.18	[core]2S(0.63)2p(1.52)3p(0.01)3d(0.01)
	N	− 1.18	[core]2S(1.37)2p(4.75)
	C	0.01	[core]2S(1.12)2p(2.85)3p(0.01)3d(0.01)
	H	0.22	1S(0.78)
	Cl	− 0.08	[core]3S(1.87)3p(5.19)3d(0.01)4p(0.01)
	F	− 0.35	[core]2S(1.85)2p(5.50)
CH ₂ ClF/BNAINS	B	1.18	[core]2S(0.63)2p(1.52)3p(0.01)3d(0.01)
	N	− 1.18	[core]2S(1.37)2p(4.75)
	Al	2.03	[core]3S(0.40)3p(0.54)3d(0.02)4p(0.01)
	C	− 0.05	[core]2S(1.16)2p(2.87)3p(0.01)3d(0.01)
	H	0.26	1S(0.74)
	Cl	0.02	[core]3S(1.86)3p(5.10)3d(0.01)4p(0.01)
	F	− 0.37	[core]2S(1.84)2p(5.52)
CH ₂ ClF/BNGaNS	B	1.18	[core]2S(0.63)2p(1.52)3p(0.01)3d(0.01)
	N	− 1.18	[core]2S(1.38)2p(4.74)
	Ga	1.82	[core]4S(0.56)4p(0.62)5p(0.01)
	C	− 0.04	[core]2S(1.15)2p(2.88)3p(0.01)3d(0.01)
	H	0.25	1S(0.75)
	Cl	0.01	[core]3S(1.86)3p(5.12)3d(0.01)4p(0.01)
	F	− 0.35	[core]2S(1.84)2p(5.50)
CH ₂ ClF	C	− 0.04	[core]2S(1.13)2p(2.89)3p(0.01)3d(0.01)
	H	0.22	1S(0.77)
	Cl	− 0.32	[core]3S(1.88)3p(5.19)3d(0.01)4p(0.01)
	F	− 0.08	[core]2S(1.84)2p(5.47)

interactions. QTAIM method was proposed by Bader et al. [70–75]. According to this theory, the critical point of the electron density, which can be a minimum point, a maximum point, or a saddle point, can fall into one of the following four categories: (1) *atomic critical point* (ACP), which denotes the geometrical position of an atom or nucleus (other than hydrogen), and geometrically represents a local maximum point of electron density in all three directions of space; (2) *bond critical point* (BCP), which indicates a critical point related to a bond or physical or chemical interaction (in reality, this point represents a saddle point with two directions of maximum electron density and one direction of minimum electron density); (3) *ring critical point* (RCP) [76, 77], which denotes a ring or set of atoms forming a ring (geometrically, it is a saddle point with the minimum electron density in one direction and

in the other two directions); and (4) *cage critical point* (CCP), which is observed when multiple rings form a cage (geometrically, this point is a local minimum point in all three directions of space). Poincaré–Hopf relationship should be satisfied to verify if all CPs may have been found as follows [78, 79]:

$$n_{(ACP)} - n_{(BCP)} + n_{(RCP)} - n_{(CCP)} = 1 \quad (21)$$

The eigenvalues of Hessian matrix, λ_1 and λ_2 , are negative and $|\lambda_1| < |\lambda_2|$ for the BCP. λ_1 and λ_2 are perpendicular to the bonding path, and λ_3 is a positive value along the bonding path. For the QTAIM analysis, is it necessary to know the electron density $\rho(r)$ and Laplacian electron density $\nabla^2 \rho(r)$. The $\rho(r)$ and $\nabla^2 \rho(r)$ play an important role in the segmentation and identification of different types of chemical interactions.

Table 6 The donor–acceptor NBO interactions and second-order perturbation energies ($E(2)$) for the CFM clusters with BNNS, BNAINS, and BNGaNS. All values obtained from completed nanosheets at the PBEPBE/6-311G(d) level of theory

Systems	Donor NBO (i)	Acceptor NBO (j)	$E(2)$ (kcal/mol)
CH ₂ ClF/BNNS	BD (B-N)	BD*(C-H)	0.07
	BD (B-N)	BD*(C-F)	0.13
CH ₂ ClF/BNAINS	BD (B-N)	LP*(Al)	14.8
	BD (B-N)	RY*(Al)	0.74
	BD (B-N)	BD*(C-Cl)	0.05
	BD (B-N)	BD*(C-H)	0.09
	BD (B-N)	BD*(C-F)	1.18
CH ₂ ClF/BNGaNS	BD (N-Ga)	BD*(C-F)	0.73
	BD (B-N)	BD*(C-H)	0.07
	BD (B-N)	BD*(C-F)	0.54
	BD (B-N)	RY*(F)	0.13
	BD (B-N)	RY*(Cl)	0.07

A BCP with negative values of $\nabla^2\rho(r)$ and large values of $\rho(r)$ (of orders exceeding 10–1 a.u.) is defined as a shared (covalent) intermolecular interaction. Also, when $\nabla^2\rho(r)$ is positive, the interactions can be classified as of the non-substrate close-shell type (which include ionic and van der Waals interactions) [80]. The elliptical bond (ϵ) [81] and the virial theorem [82] are two other important factors in the classification of bonds. An elliptical bond represents the electron density preferentially accumulated on a plate containing the bond and is defined as follows:

$$\epsilon = \frac{\lambda_1}{\lambda_2} - 1 \quad \text{where } |\lambda_1| > |\lambda_2| \quad (22)$$

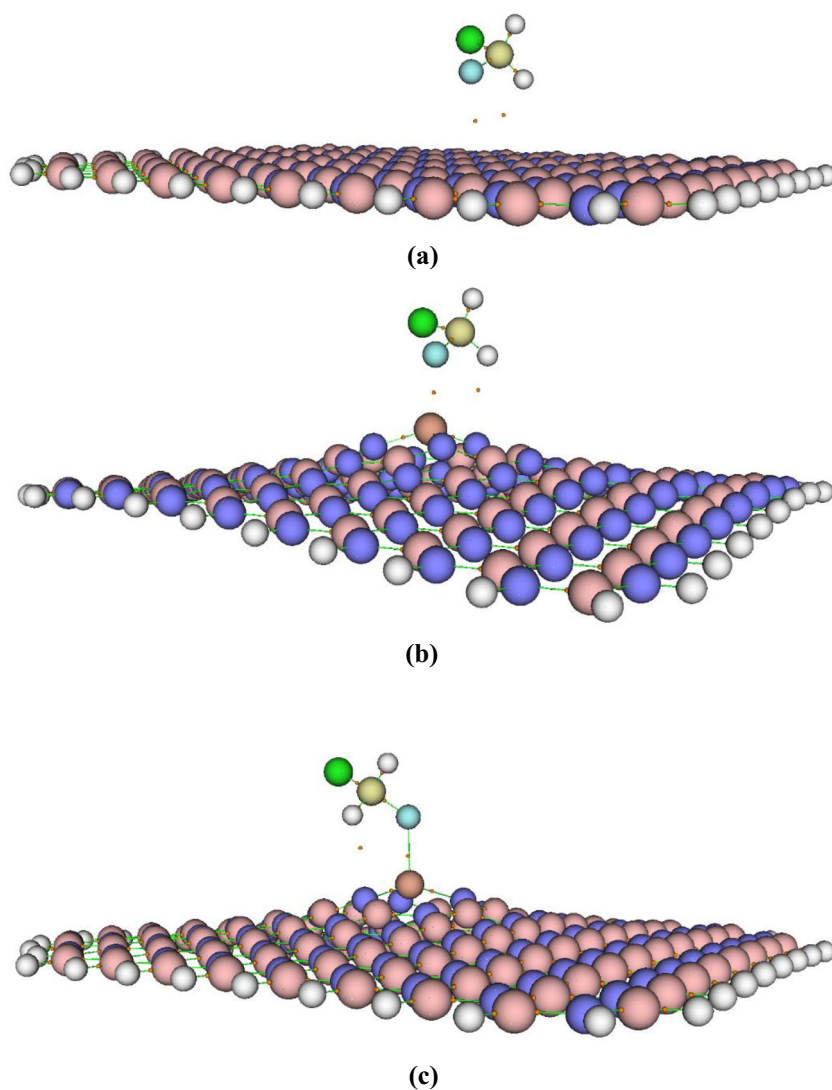
Large values of ϵ indicate an unstable structure and vice versa. Also, based on the virial theorem, the following relationship exists between the electron kinetic energy density $G(r)$ [83], the electron potential energy density $V(r)$ [84], and $\nabla^2\rho(r)$:

Table 7 The AIM topological parameters, including electron density ($\rho(r)$), Laplacian of electron density ($\nabla^2\rho(r)$), the kinetic electron density $G(r)$, potential electron density $V(r)$, eigenvalues of Hessian matrix (λ),

and bond ellipticity index (ϵ) at BCPs of the CFM clusters with BNNS, BNAINS, BNGaNS. All values have been calculated using the B3LYP-D3/6-311G(d) level of theory from NBO analysis

Systems	Bond	ρ	∇^2r	$G(r)$	$V(r)$	$G(r)/V(r)$	λ_1	λ_2	λ_3	ϵ
CH ₂ ClF	C–H	0.2788	−0.9946	0.0287	−0.3061	0.0939	−0.7828	−0.7617	0.5499	0.0277
	C–Cl	0.1765	−0.1940	0.0597	−0.1680	0.3557	−0.2799	−0.2657	0.3517	0.0532
	C–F	0.2550	−0.1198	0.3286	−0.6872	0.4782	−0.4988	−0.4292	0.8082	0.1621
BNNS	B–N	0.1923	0.4258	0.2717	−0.4370	0.6218	−0.4516	−0.4440	1.3215	0.0171
BNAINS	Al–N	0.1137	0.8632	0.2269	−0.2380	0.9534	−0.2090	−0.1848	1.2571	0.1309
BNGaNS	Ga–N	0.1533	0.7746	0.2501	−0.3066	0.8158	−0.2317	−0.2230	1.2294	0.0389
CH ₂ ClF/BNNS	F...N	0.0067	0.0276	0.0057	−0.0046	1.2553	−0.0049	−0.0016	0.0342	1.9883
	C...N	0.0042	0.0154	0.0030	−0.0021	1.4129	−0.0025	−0.0012	0.0191	1.1781
	B–N	0.0142	0.0535	0.0113	−0.0093	1.2180	−0.0160	−0.0112	0.0806	0.4270
	C–H	0.2836	−1.0464	0.0264	−0.3145	0.0841	−0.8105	−0.7885	0.5526	0.0280
	C–Cl	0.2489	−0.0817	0.3292	−0.6788	0.4850	−0.4939	−0.4134	0.8256	0.1948
	C–F	0.2823	−1.0316	0.0270	−0.3120	0.0867	−0.8028	−0.7801	0.5513	0.0290
CH ₂ ClF/BNAINS	F...Al	0.0345	0.2035	0.0494	−0.0479	1.0310	−0.0433	−0.0424	0.2892	0.0228
	C...N	0.0117	0.0361	0.0080	−0.0070	1.1412	−0.0107	−0.0070	0.0538	0.5237
	Al–N	0.1002	0.7011	0.1831	−0.1910	0.9590	−0.1735	−0.1594	1.0340	0.0882
	B–N	0.1960	0.4614	0.2841	−0.4529	0.6274	−0.4641	−0.4485	1.3741	0.0348
	C–H	0.2859	−1.0849	0.0248	−0.3207	0.0772	−0.8288	−0.8038	0.5476	0.0311
	C–Cl	0.2020	−0.2983	0.0649	−0.2044	0.3176	−0.3349	−0.3197	0.3563	0.0473
CH ₂ ClF/BNGaNS	C–F	0.1941	−0.1077	0.2047	−0.4363	0.4691	−0.3003	−0.2359	0.4285	0.2731
	F...Ga	0.0479	0.2047	0.0596	−0.0681	0.8757	−0.0559	−0.0543	0.3150	0.0295
	C...N	0.0099	0.0312	0.0068	−0.0058	1.1666	−0.0086	−0.0047	0.0445	0.8147
	Ga–N	0.1327	0.6356	0.2016	−0.2444	0.8251	−0.1893	−0.1828	1.0077	0.0354
	B–N	0.1963	0.4824	0.2881	−0.4556	0.6324	−0.4663	−0.4506	1.3993	0.0347
	C–H	0.2855	−1.0772	0.0252	−0.3197	0.0788	−0.8247	−0.8002	0.5477	0.0305
	C–Cl	0.1973	−0.2817	0.0633	−0.1970	0.3212	−0.3263	−0.3105	0.3551	0.0510
	C–F	0.2069	−0.1074	0.2345	−0.4958	0.4729	−0.3391	−0.2691	0.5008	0.2600

Fig. 6 AIM molecular graphs for **a** CFM/BNNS, **b** CFM/BNAINS, and **c** CFM/BNGaNS systems. Orange dots represent the boundary critical points (BCPs)



$$\frac{1}{4}\nabla^2\rho(r) = 2G(r) + V(r) \quad (23)$$

The balance between $G(r)$ and $V(r)$ reflects the nature of the interaction, and therefore, the ratio of $G/|V|$ can be used as an appropriate index in link classification. If this ratio is less than 0.5, the nature of the interaction will be purely covalent, and if the ratio is greater than 1, the interaction may be considered completely non-covalent. Note that for covalent bonds (i.e., $\nabla^2\rho(r) < 0$ and $G/|V| < 0.5$), the nature of the bond changes from van der Waals interactions to strong covalent interactions. It becomes covalent. It can also play a decisive role in controlling the amount of ionic interaction for close-shell interactions (i.e., $\nabla^2\rho(r) > 0$ and $G/|V| > 1$), as they become stronger ionically (and weakly electrostatic) by reducing interactions. Therefore, the QTAIM topology analysis together

with WBI analysis and adsorption results expose an important trend: by increasing the ionic character of atomic bonds in the nanosheets, the tendencies of the gases to adsorb are also increased.

Considerable results can be obtained from reviewing Table 7. It is observed that in all adsorption sites Laplacian of electron energy density has a positive value; that is, the bond is noncovalent. In the study of doped systems, we found that for the all clusters the energy density and the energy density of Laplacian are high indicating that there is a strong bond between the nanosheets and the CFM molecule and the elliptical bond is close to 0, which means the interaction is strong. As stated above, when the ratio of $G/|V|$ is more than 1, it means non-covalent bonding, in the case of Ga-doped clusters these amounts are less than 1. In other words, the results of QTAIM analysis also confirm the strong adsorption of the CFM molecule on the BN(Al)NT and BN(Ga)NT (Fig. 6).

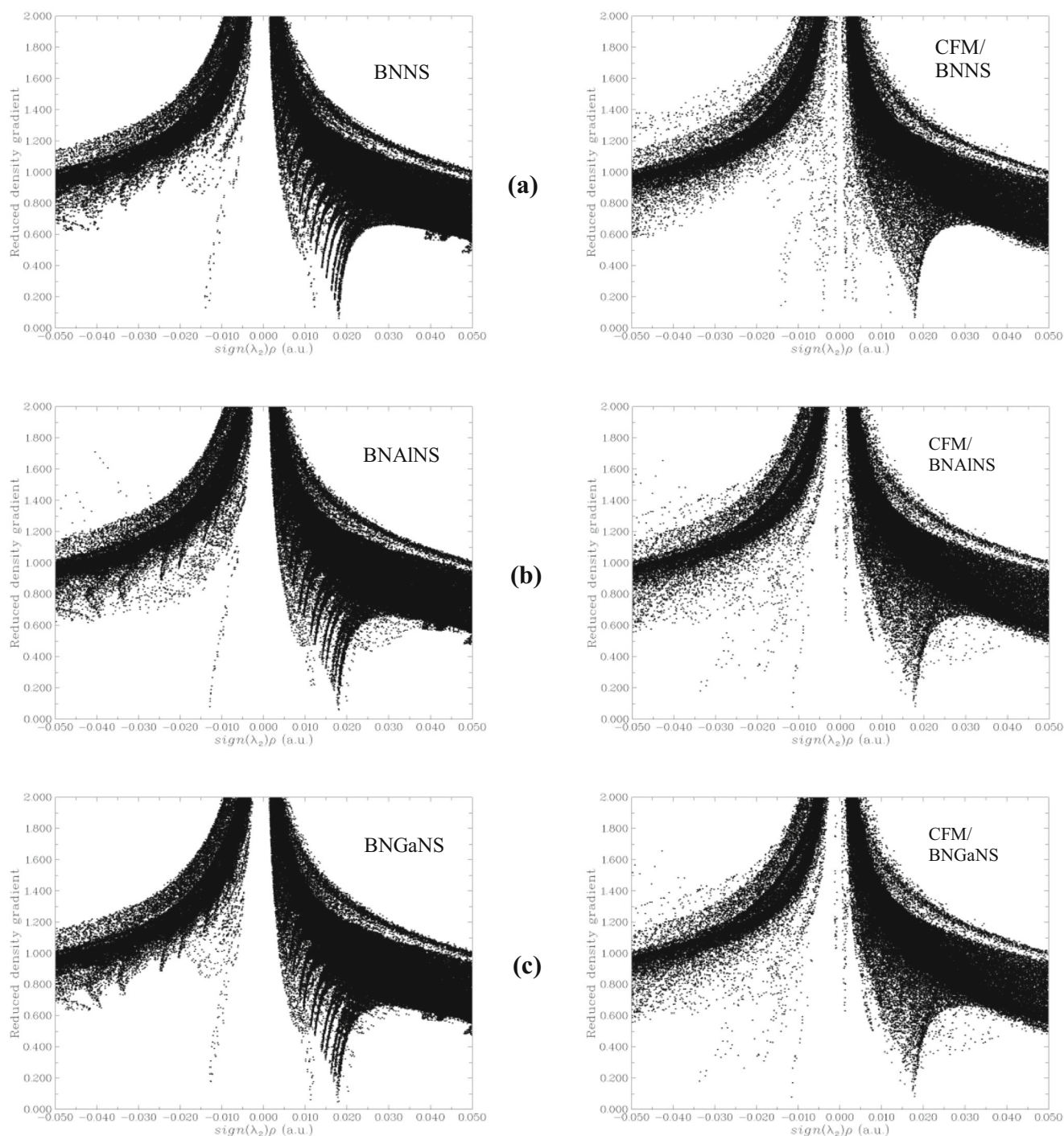


Fig. 7 Plots for the reduced density gradient (RDG) vs. $\text{sign}(\lambda_2)\rho(r)$ values of the **a** pristine **b** Al-doped, and **c** Ga-doped boron nitride nano-sheets. The data were obtained from completed nanosheet and B3LYP-

D3 /6-311G(d) level of theory. The left side diagrams are isolated nano-sheets and the right side diagrams are CFM/nanosheet clusters

The reduced density gradient (RDG) function and $\text{sign}(\lambda_2)\rho(r)$ are used to evaluate the weak interactions. These functions are categorized in the context of non-covalent interaction methods which is powerful way to analyze the types of intermolecular interactions. The RDG is defined as follows [85, 86]:

$$\text{RDGs} = \frac{1}{2(3\pi^2)^{\frac{1}{3}}} \frac{|\overline{\Delta\rho(r)}|}{\rho(r)^{\frac{4}{3}}} \quad (24)$$

The strength of the interaction has a positive correlation with electron density $\rho(r)$ and the second largest eigenvalue

of the Hessian matrix (λ_2). Thus, the real space function $\text{sign}\lambda_2(r)\rho(r)$ (the products of the signs of λ_2 and ρ) can be defined. The scatter graph of the sign of the $\lambda_2(r)\rho(r)$ function (X-axis) and RDG (Y-axis) reveals the interaction type between gases and nanosheets. The RDG values range from medium to very large around the nuclei and edges of the molecules, whereas weak interactions (zero to medium) are observed around the chemical bonds. Also, for each specific value of RDG (seen as a horizontal line on the graph), the regions of the graph can be classified into three types, namely, $\text{sign}\lambda_2(r)\rho(r) < 0$ (strong attraction), $\text{sign}\lambda_2(r)\rho(r) \approx 0$ (weak van der Waals interaction), and $\text{sign}\lambda_2(r)\rho(r) > 0$ (strong repulsion (steric effect in ring)) [85, 86].

Using the isosurface $\text{RDG} = 0.5$ as a reference, it can be concluded that after adsorption of the gas onto the outer surfaces of the nanosheets, spots appeared around the region characterized by $\text{sign}\lambda_2(r)\rho(r) \approx 0$. The interaction of gas with BN nanosheets is in the range of strong van der Waals interactions in nature. Significant changes in the overall features of the pristine nanosheet graph (Fig. 7) after the adsorption of gases were observed in the region characterized as $\text{sign}\lambda_2(r)\rho(r) < 0$ (i.e., strong attraction), implying that the nanosheet/gas interactions were strong. Hence, this analysis also confirms the results of the single-point energy calculations and NBO analysis, namely that the interactions of CFM with BNNS, BNAINS, and BNGaNS were strong.

Conclusions

In this study, the interactions between chlorofluoromethane molecule and pristine, and Al- and Ga-doped boron nitride nanosheets were investigated using density functional framework. To this end, the structure of the nanosheets and CFM molecule was optimized at the theoretical level of PBE-PBE/6-311G (d). Right after that, B3LYP-D3, M062X, and wB97XD functionals and same basis set were also used to consider the contribution of long-range interactions and dispersion effect. QTAIM and NBO analyses were also implemented to consider the character of intermolecular interactions. The results of all analyses are in agreement and show the following: (1) among the different positions studied for pristine boron nitride nanosheet, the T_3 position has the highest absorption energy; (2) investigations in this study show that the Al and Ga elements can be substituted by BNNS nanosheet atoms by chemical bonding and, as a binding element, cause dramatic changes in the chemical, electronic, and mechanical structure of BNNS nanosheets; (3) among the doped nanosheets, Ga-doped BNNS has a very high adsorption energy compared with other elements, and is expected to be chemically adsorbed in this case and appears to be a suitable sensor characteristic option. The next category is Al element, where the adsorption energy is higher than the initial

state but lower than that of Ga. Generally, we found that the adsorption tendencies of the aforementioned gas molecule have a positive correlation to the nature of the bonds in BN nanosheets. Finally, we, according to the results obtained from energy gap and adsorption energies, conclude that the BNNS, BNAINS, and BNGaNS are favorable candidates for utilization as gas sensor devices to detect CFM molecule.

Acknowledgments The authors would like to thank the Solid-State Theory Group at the Physics Department at the Università degli Studi di Milano-Italy for providing computational facilities.

Compliance with ethical standards

Conflict of interest The authors declare that they have no conflict of interest.

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